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**QUANTITATIVE TECHNIQUES**

November 2022

Time: 3 hours

**THE KENYA NATIONAL EXAMINATIONS COUNCIL****DIPLOMA IN PROJECT MANAGEMENT  
DIPLOMA IN MARITIME TRANSPORT LOGISTICS  
DIPLOMA IN DISASTER MANAGEMENT****QUANTITATIVE TECHNIQUES****3 hours****INSTRUCTIONS TO CANDIDATES**

*This paper consists of SEVEN questions.*

*Answer any FIVE questions in the answer booklet provided.*

*Show all your working.*

*Candidates should answer the questions in English.*



**This paper consists of 5 printed pages.**

**Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.**

- ✓ (a) Explain five ways in which quantitative techniques may be applied in business decision making. (10 marks)
- (b) The following are the ranks awarded by 3 judges to 10 employees in a performance contest:

| Employee | Ranks Awarded |         |         |
|----------|---------------|---------|---------|
|          | Judge 1       | Judge 2 | Judge 3 |
| A        | 5             | 6       | 5       |
| B        | 7             | 3       | 1       |
| C        | 1             | 5       | 6       |
| D        | 6             | 2       | 8       |
| E        | 2             | 4       | 7       |
| F        | 8             | 7       | 10      |
| G        | 3             | 10      | 2       |
| H        | 10            | 9       | 4       |
| I        | 4             | 1       | 9       |
| J        | 9             | 8       | 3       |

- (i) Calculate the Spearman's rank coefficient of correlation for each pair of judges.
- (ii) Determine the most consistent pair of judges.

(10 marks)

2. (a) Explain four benefits of time series analysis in business decision making. (8 marks)

- (b) A company manufactures two products; A and B. The two products pass through three machines; I, II and III. The following information relates to the two products and the three machines.

|                 | Number of hours per unit |    | Available Number of hours |
|-----------------|--------------------------|----|---------------------------|
|                 | A                        | B  |                           |
| Machine I       | 5                        | 2  | 1000                      |
| Machine II      | 3                        | 2  | 900                       |
| Machine III     | 1                        | 2  | 500                       |
| Profit per unit | 100                      | 40 |                           |

- (i) Formulate the linear programming problem.



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$$F = \frac{P_A Q_A}{P_B Q_B} \times \frac{P_C Q_C}{P_D Q_D} \times 100$$

$$F = \frac{P_A Q_A}{P_B Q_B} \times 100$$

$$L = \frac{2y - 2x}{\sqrt{2^2 + 2^2}} \times g^2 (y)^2$$

(ii) Using the graphical method:

Determine the:

- (I) number of units of each product to be produced.  
 (II) maximum profit.

(12 marks)

3/ (a) Given the following matrices:

$$A = \begin{pmatrix} 2 & -2 \\ 6 & 10 \end{pmatrix}, B = \begin{pmatrix} 2 & 0 \\ 8 & -4 \end{pmatrix} \text{ and } C = \begin{pmatrix} 6 & -7 \\ 8 & 3 \end{pmatrix}$$

Determine:

- (i)  $C^T - 3(B + \frac{1}{2}A)$   
 (ii)  $(AB)^T$   
 (iii) determinant of C.

(10 marks)

(b) The following are the prices and quantities of four commodities for the years 2014 and 2018.

| Commodity | 2014             |                        | 2018             |                        |
|-----------|------------------|------------------------|------------------|------------------------|
|           | Prices<br>(Ksh.) | Quantities<br>(tonnes) | Prices<br>(Ksh.) | Quantities<br>(Tonnes) |
| A         | 20               | 200                    | 25               | 180                    |
| B         | 40               | 150                    | 50               | 120                    |
| C         | 50               | 200                    | 75               | 150                    |
| D         | 100              | 320                    | 120              | 280                    |

Calculate the:

- (i) Laspayre's quantity index;  $\frac{\sum p_0 q_1}{\sum p_1 q_1} \times 100$   
 (ii) Paasche's quantity index;  
 (iii) Fisher's ideal quantity index.

(10 marks)



- A. (a) The following information shows the profits made by a company in millions of shillings for 10 consecutive years.

| Year | Profit<br>(Ksh. millions) |
|------|---------------------------|
| 2004 | 20                        |
| 2005 | 25                        |
| 2006 | 22                        |
| 2007 | 30                        |
| 2008 | 60                        |
| 2009 | 55                        |
| 2010 | 90                        |
| 2011 | 85                        |
| 2012 | 100                       |
| 2013 | 120                       |

Handwritten calculations for least squares method:

$$\sum x = 10, \sum y = 500, \sum xy = 3200, \sum x^2 = 55$$

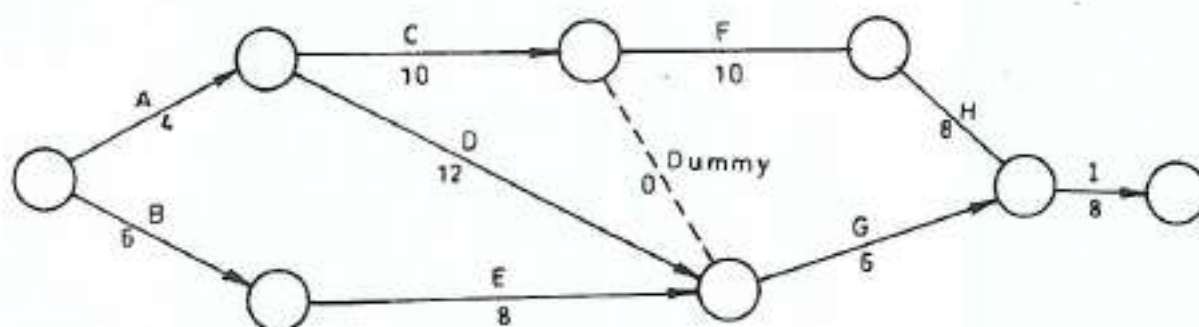
$$a = \frac{\sum y - b \sum x}{n} = \frac{500 - 30 \cdot 10}{10} = 20$$

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2} = \frac{10 \cdot 3200 - 100 \cdot 500}{10 \cdot 55 - 100} = \frac{32000 - 50000}{550 - 100} = \frac{-18000}{450} = -40$$

- (i) Using the least squares method, determine the trend line equation.  
 (ii) Using the equation in (i) above, estimate the profit of the company for the year 2020.

(10 marks)

- (b) The following is a network diagram of a project to be undertaken by a company. The activity durations are given in weeks.



- (i) Prepare a precedence table showing activity, preceding activities and activity duration.  
 (ii) Determine the:
- critical path;
  - project duration.

Activity  
A  
B  
C  
D  
E  
F  
G  
H

(10 marks)





5. (a) Describe the steps followed in the test of a hypothesis. (10 marks)
- (b) At Kendu Limited, 30% of the employees have a degree qualification. A random sample of 10 employees was selected from the company. Determine the probability that:
- three employees had a degree qualification;
  - no employee had a degree qualification;
  - at least one employee had a degree qualification;
  - at most two employees had a degree qualification.

(10 marks)

6. (a) Explain five categories of inventories that may be held by a firm. (10 marks)

- (b) The following is the Marginal Revenue (MR) function of a firm.

$$MR = 160 - 0.2q;$$

where  $q$  is the level of output sold. Determine the:

- total revenue function;
- average revenue function;
- level of output that will maximize total revenue;
- maximum total revenue;
- price at maximum total revenue.

(10 marks)

7. (a) Explain five limitations of index numbers. (10 marks)

- (b) Joshua has received terminal benefits amounting to Ksh 2,000,000. He is considering investing this amount for a period of 5 years under either of the following options:

**Option I**

Invest in a bank account paying compound interest at the rate of 14% per annum.

**Option II**

Invest in a mutual fund paying interest at the rate of 10% per annum, compounded semi-annually.

- Determine the amount in his account at the end of 5 years under each of the options.
- Calculate the interest earned under each option.
- Based on the results in (i) above, advise Joshua on the option under which to invest.

(10 marks)

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